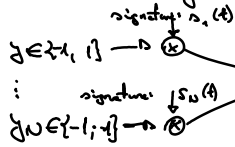
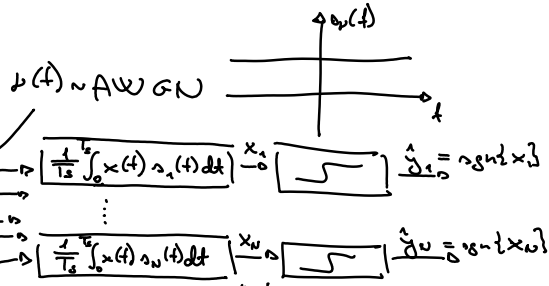


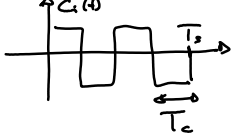
Multi user systems:



Radio Channel



code: $c^{(i)} = (1; -1; 1; -1)$

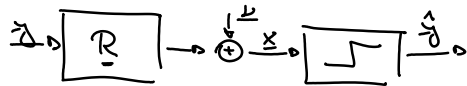


$$x(t) = \sum_{i=1}^M y_i s_i(t) + \nu(t) \rightarrow \text{user } i \text{ e}$$

more precise model: $x(t) = \sum_{i=1}^M y_i s_i(t - T_i) + \nu(t)$

most precise model: $x(t) = \sum_{i=1}^M y_i h_i(t - T_i) * s_i(t) + \nu(t)$

$$\left. \begin{array}{l} \frac{1}{T_s} \rightarrow \text{data speed} \\ T_c : \text{handover} \end{array} \right\} N = \frac{T_s}{T_c} = \frac{\text{service}}{\text{HW}}$$



$$x = R y + \nu; \quad R_{e_i} = \frac{1}{T_s} \int_0^{T_s} s_e(t) s_i(t) dt = \frac{1}{N} \sum_{n=1}^N c_n^{(e)} c_n^{(i)} = \frac{1}{N} c^{(e)T} c^{(i)}$$

$$R_{ee} = 1 \quad \forall e$$

$$x_e = \sum_{i=1}^M R_{ei} y_i + \nu_e = R_{ee} y_e + \sum_{i=1, i \neq e}^M R_{ei} y_i + \nu_e = y_e + \underbrace{\sum_{i=1, i \neq e}^M R_{ei} y_i}_{\text{Multi User Interference}} + \nu_e$$

Multi User Interference
MUI

Best case: $MUI = 0 \Rightarrow R_{ei} = 0 \quad \forall i = 1 \dots M, i \neq e$

$c^{(e)}, e = 1 \dots M \rightarrow$ orthogonal vector set $\rightarrow \dim(c^{(e)}) = N > M \iff M > N$

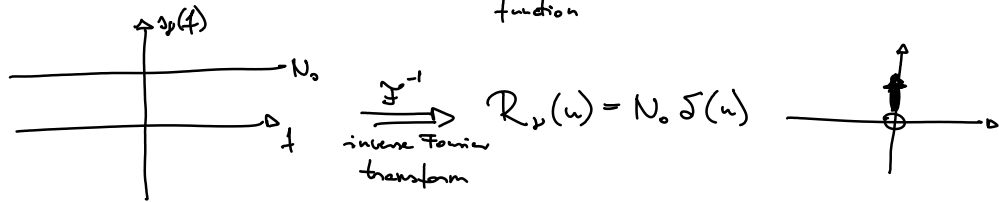
\Rightarrow Because of that constraint, it is impossible to set MUI to 0

$$\nu; \quad x_e = \frac{1}{T_s} \int_0^{T_s} \nu(t) s_e(t) dt, \quad e = 1 \dots M \rightarrow \nu \sim \mathcal{N}(0, K)$$

$$K_{e_i} = E\{\nu_e \nu_i\} = E\left\{ \frac{1}{T_s} \int_0^{T_s} \nu(t) s_e(t) dt \cdot \frac{1}{T_s} \int_0^{T_s} \nu(\tau) s_i(\tau) d\tau \right\} = E\left\{ \frac{1}{T_s^2} \int_0^{T_s} \int_0^{T_s} \nu(t) \nu(\tau) s_e(t) s_i(\tau) dt d\tau \right\}$$

$$= \frac{1}{T_s^2} \int_0^{T_s} \int_0^{T_s} E\{\nu(t) \nu(\tau)\} s_e(t) s_i(\tau) dt d\tau = \frac{1}{T_s^2} \int_0^{T_s} \int_0^{T_s} R_{\nu}(t-\tau) s_e(t) s_i(\tau) dt d\tau = (*)$$

autocorrelation - function



$$(*) = \frac{N_0}{T_s} \frac{1}{T_s} \int_0^{T_s} s_e(t) s_i(t) dt = N_0' R_{e_i}$$

$$P_{\nu}(\omega) = \frac{1}{(2\pi)^M \det(N_0' R)} e^{-\omega^T N_0' R^{-1} \omega}$$

$$e^{-\frac{1}{2} x^T N_0^{-1} R^{-1} x}$$

Review x

$$\hat{y} = \max_{y \in \{-1, 1\}^n} P(y|x) \sim \max_{y \in \{-1, 1\}^n} \frac{P(x|y) P(y)}{P(x)} \sim \max_{y \in \{-1, 1\}^n} P(x|y)$$

$$\hat{y} = \max_{y \in \{-1, 1\}^n} \frac{1}{\sqrt{(2\pi)^n \det(N_0^{-1} R^{-1})}} e^{-\frac{1}{2} (x - R y)^T N_0^{-1} R^{-1} (x - R y)} \sim \max_{y \in \{-1, 1\}^n} -\frac{1}{2} (x - R y)^T N_0^{-1} R^{-1} (x - R y) \sim$$

just a constant...

$$\sim \min_{y \in \{-1, 1\}^n} (x - R y)^T R^{-1} (x - R y) \sim \min_{y \in \{-1, 1\}^n} x^T R^{-1} x - y^T \overbrace{R^T R^{-1}}^I x - x^T \overbrace{R^{-1} R}^I y + y^T \overbrace{R^T R^{-1} R}^I y \sim$$

$$\sim \min_{y \in \{-1, 1\}^n} y^T R y - 2 x^T y \Rightarrow \text{Multi User Detection Problem}$$

✓ beyond 3G

B3G mobile communication:

