



$$x_e = \frac{1}{T_s} \int_0^{T_s} x(t) s_e(t) dt = \frac{1}{T_s} \int_0^{T_s} \left( \sum_{i=1}^M y_i s_i(t) + \nu(t) \right) s_e(t) dt = \sum_{i=1}^M y_i \frac{1}{T_s} \int_0^{T_s} s_e(t) s_i(t) dt + \frac{1}{T_s} \int_0^{T_s} \nu(t) s_e(t) dt$$

$$R_{ei} = \frac{1}{T_s} \int_0^{T_s} s_e(t) s_i(t) dt = \frac{1}{N} \sum_{m=1}^N c_m^{(e)} \cdot c_m^{(i)} = \frac{1}{N} c^{(e)T} c^{(i)}$$

$$\nu_e = \frac{1}{T_s} \int_0^{T_s} \nu(t) s_e(t) dt; \quad x_e = \sum_{i=1}^M R_{ei} y_i + \nu_e \quad ; \quad e = 1 \dots M$$

$$\vec{x} = \mathbf{R} \vec{y} + \vec{\nu}$$

$$x_e = R_{ee} y_e + \sum_{i \neq e} R_{ei} y_i + \nu_e$$

MUI: multi user interference  $\Rightarrow$  our enemy that we want to destroy  $\Rightarrow$  let set  $R_{ei} = 0 \quad \forall i \neq e \Rightarrow$  choose orthogonal codes

$$\hat{y}_e = \text{sgn} \left\{ R_{ee} y_e + \sum_{i \neq e} R_{ei} y_i + \nu_e \right\}$$

$$R_{ei} = 0 = \frac{1}{N} \sum_{n=1}^N c_n^{(e)} c_n^{(i)} = \frac{1}{N} c^{(e)T} c^{(i)}$$

$i = 1 \dots M, i \neq e$   
 $M < N = \frac{T_s}{T_c} \rightarrow 6 \text{ (high speed serial)}$   
 $\rightarrow 1000 \text{ (voice)}$

Walsh-Hadamard construction:

$$\left. \begin{aligned} \underline{H}_{2 \times 2} &= \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix} \\ \underline{H}_{4 \times 4} &= \begin{bmatrix} \underline{H}_{2 \times 2} & \underline{H}_{2 \times 2} \\ \underline{H}_{2 \times 2} & -\underline{H}_{2 \times 2} \end{bmatrix} \\ \dots \\ \underline{H}_{(N \times N) \times (N \times N)} &= \begin{bmatrix} \underline{H}_{N \times N} & \underline{H}_{N \times N} \\ \underline{H}_{N \times N} & -\underline{H}_{N \times N} \end{bmatrix} \end{aligned} \right\} M < 2^L \rightarrow \text{Challenge of 3G}$$